A. Teaching notes for the guided questions of Simulation III

	Center of Mass	Male Re	f. %	Female	Ref.	%	Sim.	%	
	cgf/f		43.0		43	8.4	43	3.2	
	cgu/u		43.6		45	5.8	44	4.7	
ł	Body Parameters	s Male R	ef. %	6 Femal	e Ref.	. %	Sim	. %	
	W_{FA}/W_P		2.5	5		2.1	-	2.3	,
	W_{UA}/W_P		3.3	3		2.9		3.1	
	f/H_P		21.5	5	2	21.8	3 2	21.6)
	u/H_P		17.2	2	1	7.3	;]	17.3	,
	b/f		_	-		_	· 1	11.0	1
	d/(f+u)		_	-		_		25.0	ĺ

Simulation III employs the parameters in Table I.

TABLE I. Parameters of the human segments in reference and in our Simulation III (the average of male and female).^{1,2} The first table is for the positions of center of mass. The bottom table shows the weight and length ratios of body segments as well as the muscle insertions.

• "How do the forces on biceps and elbow joint change with different angles of their elbow bending when $\theta_{arm} = 0^{\circ}$? Does the change become different for people with different BMI?"

When $\theta_{arm} = 0^{\circ}$, the calculation of the forces on biceps and elbow joint is suggested with a given value of $\theta_u(>90^{\circ})$ before this guided question. The difficulty level of the calculation is moderate when the lever arm value of F_{bic} is given. This calculation practice can help students have deep understanding when they move to the guided question and give reasonable explanation of what they discovered from the simulation.

Both forces on biceps and elbow joint are at a minimum when $\theta_u = 90^{\circ}$ and the forces increase symmetrically when θ_u departs from 90°. Similarly to one of the guided questions in Simulation II, people with larger BMI always experience larger forces, although the difference is less pronounced for the biceps and elbow.

- "Most forces except F_{del} have the lowest values when the forearm remains vertical while the shoulder extends and flexes. What is the reason behind it?"
- "What are the optimal and most challenging poses for lifting objects? What is the range of each force experienced for different poses of their arm?" Hint: control variables. Fix one of the two variables θ_{arm} (90°, 90°) and θ_u (30°, 180°), then explore the force change with the other. The range of the second variable is also restricted by the condition $\theta_u \theta_{arm} > 90^\circ$, where bicep force plays the major role of maintain balance.

The sequence of guided questions is designed to encourage students to adapt their reasoning from one question to the next. Starting with a simple case where the upper arm is horizontal in the first guided question, it is straightforward for the students to geometrically connect that the zero lever arms of the weight of the ball and the weight of the forearm are the reason for the most comfortable position when the forearm is upright and to realize the role of lever arm in equilibrium. Moving to the second question, it leads the students to conclude the same reason that the easiest positions always have the forearm upright. In teaching practice, the last question can be assigned for assignments for extra credits.

¹ Stanley Plagenhoef, F. Gaynor Evans and Thomas Abdelnour, "Anatomical data for analyzing human motion," Res. Q. Exerc. Sport," 54, 169–178 (1983).

² Howard D. Goldick, Mechanics, Heat and the Human Body: An Introduction to Physics, (Pearson, New Jersey, 2001), p. 99.

Derivations of the equations in the manuscript "Interactive simulations of upper limbs" The three cases represent different configurations of upper limbs, the upper arm and forearm above and below the horizon. "u" and "f" are the lengths of upper arm and forearm. Weight of a ball, W_bal acts on the end of the forearm.

case LAbali = f. sin Ox Eq(5)Same metrical $90^{\circ} - \theta_{x} = 360^{\circ} - \theta_{u} - (180^{\circ} - \theta_{arm})$ analysis for to $\theta_{\rm X} = \theta_{\rm u} - \theta_{\rm arm} - 90^{\circ}$ shoulder (ase $\theta_u - \theta_{arm} + (90^\circ - \theta_x) = 180^\circ$ $\theta_{\rm X} = \theta_{\rm u} - \theta_{\rm arm} - 90^{\circ}$ (ase 3 2-Oarm 11 Ou $\theta_{\mu} = A_{x} + (90^{\circ} + \theta_{arm})$ $\Theta_{\rm X} = \Theta_{\rm H} - \Theta_{\rm arm} - 90^{\circ}$ 90-(- (avm) Method 1. shoulder $(u^2_{+b})^2 - 2ub \cos \theta_u) + b^2 - 2\sqrt{u^2_{+b}}^2 - 2ub \cos \theta_u \cdot b \cdot \cos \theta_b = u^2$ U.Sin [180°-Qu) U $uo3\theta_{b}^{\prime} = \frac{2b^{2} - 2ub\cos\theta_{u}}{2\sqrt{u^{2} + b^{2} - 2ub\cos\theta_{u}} \cdot b} = \frac{b - uo3\theta_{u}}{\sqrt{u^{2} + b^{2} - 2ub\cos\theta_{u}}}$ $9_{b} = 180^{\circ} - 9_{b}'$ check the triangle area Method 2 $b \cdot u \sin (180^\circ - \theta_u) = \sqrt{u^2 + b^2 - 2ub \cdot cos \theta_u} \cdot b \cdot sin \theta_b$ $Sin \theta_b = \frac{u sin \theta_u}{\sqrt{u^2 b^2 - 2ubros \theta_u}}$ Eq(7) for Ob JRFel=Fbic 103 By case $(\mathcal{O}_u - \mathcal{O}_{arm}) \dagger \mathcal{O}_y = \mathcal{O}_b \qquad \therefore \mathcal{O}_y = \mathcal{O}_b - \mathcal{O}_u \dagger \mathcal{O}_{arm}$ JRFeh = Fbic COSOY = Fbic COS(-By) Eq.(8) = Fbic cos (- Darm + Qu - Ph) JRFev = Fbic STA By + WFA+ Wbat = Fbic STA (Ob-Out Oarm) + WFA + Whad

= - Fbic Sin (-Oarin + Ou-Ob) + WFA+ Wbal



 $-\partial_{arm} + \partial_{u} = \partial_{b} + \partial_{y} = \partial_{arm} + \partial_{u} - \partial_{b}$ Fbic sin By + JRFev = WFA + Wbal JRFev = -Fbic STON Oy + WFAt Wbal = -Fbic STON (-Oarm + Ou - Ob) + WF + Wbal JRFeh= Fbic (05 By = Fbic (05 (-Darm+Bu-Ob) Eq(8

case 3

P. Flic Ob

 $\theta_h = \theta_u + (\theta_{arm} - \theta_y)$: Qy = - Darm + Qu-Db



$$rase 1$$

$$JRF_{sh} = F_{bic} \cdot ros \theta_{y} + F_{del} \cdot ros \theta_{z}$$

$$JRF_{sh} = F_{del} \cdot ros \theta_{z} + F_{bic} \cdot ros \theta_{y}$$

$$F_{bic} \cdot ros \theta_{y}$$

JRFsv + Fidel Son Or = Fbic Son Oy + WFA + WWA + Wbal JRFsv = - Fidel Son Oz + Fbic Son Oy + WFA + WWA + Wbal W Fidel Son (-Or) Eq(8). case 1 W : JRFsv = Fidel Son (Oarm - Odel) - Fbic (- Oarm + Ou - Ob) + WFA + WWA + Wbal

$$(ased)$$

$$JRF_{sv}$$

$$-Gavm + Gdel$$

$$JRF_{sh} = Fdel \cdot (\sigma_{s} G_{z} + Fdel \cdot (\sigma_{s} G_{y} + Fdel \cdot (\sigma_{s} + Fdel \cdot (\sigma_{s$$

Shoulder Darm

Ou = 90° + Oarm Ou = 90° + Oarm Ou - Oarm = 90° when the forearm goes counter clock wise, even with a small congle bicep force is not the reason of keep equilibrium.

- Carm Ou

same for this case $\theta_u + (-\theta_{arm}) = 90^\circ$